# Microwave-Based Structure and Four-Dimensional Morphed Intermolecular Potential for $\mathrm{HI}-\mathrm{CO}_{2}$ 

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Received: June 7, 2007; In Final Form: July 20, 2007


#### Abstract

Microwave spectra of the four isotopologue/isotopomers, $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}, \mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}, \mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$, and $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$, have been recorded using pulsed-nozzle Fourier transform microwave spectroscopy. In the last two isotopomers, the heavy oxygen atom tilted toward and away from the HI moiety, respectively. Only $b$-type $K_{\mathrm{a}}=1 \leftarrow 0$ transitions were observed. Spectral analysis provided molecular parameters including rotational, centrifugal distortion, and quadrupole constants for each isotopomer. Then, a four-dimensional intermolecular energy surface of a $\mathrm{HI}-\mathrm{CO}_{2}$ complex was generated, morphing the results of ab initio calculations to reproduce the experimental data. The morphed potential of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ had two equivalent global minima with a well depth of $457(14) \mathrm{cm}^{-1}$ characterized by a planar quasi-T-shaped structure with the hydrogen atom tilted toward the $\mathrm{CO}_{2}$ moiety, separated by a barrier of $181(17) \mathrm{cm}^{-1}$. Also, a secondary minimum is present with a well depth of $405(14) \mathrm{cm}^{-1}$ with a planar quasi-T-shaped structure with the hydrogen atom tilted away from the $\mathrm{CO}_{2}$ moiety. The ground state structure of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ was determined to have a planar quasi-T-shaped geometry with $R=3.7717(1) \AA, \theta_{\mathrm{OCI}}=82.30(1)^{\circ}, \theta_{\mathrm{CIH}}=71.55(1)^{\circ}$. The morphed potential obtained is now available for future studies of the dynamics of photoinitiated reactions of this complex.


## 1. Introduction

There has been considerable interest in using weakly bound binary complexes for investigating the dynamics of elementary chemical reactions. ${ }^{1}$ In particular, the following reaction has been extensively studied. ${ }^{2-9}$

$$
\begin{equation*}
\mathrm{H}+\mathrm{CO}_{2} \rightarrow[\mathrm{HOCO}]^{\ddagger} \rightarrow \mathrm{OH}+\mathrm{CO} \tag{1}
\end{equation*}
$$

In such studies, the reactants H and $\mathrm{CO}_{2}$ have been prepared in situ by photodissociating the HX bond in an $\mathrm{H}_{n} \mathrm{X}: \mathrm{CO}_{2}$ complex ( $\mathrm{X}=\mathrm{I}, \mathrm{Br}, \mathrm{Cl}, n=1$, and $\mathrm{X}=\mathrm{S}, n=2$ ) and the product OH has been probed. As a consequence, these investigations have led to further understanding of the influence of the nearby spectator X atom on such reactions. It has been pointed out that Van der Waals forces as well as large-amplitude zero-point motion of the HX monomer are responsible for governing the initial orientation of the reactants and should be considered in the interpretation of the experimental results. Furthermore, detailed structural studies of the $\mathrm{HX}: \mathrm{CO}_{2}$ complexes $(\mathrm{X}=\mathrm{F}, \mathrm{Cl} \text {, and } \mathrm{Br})^{10-13}$ have greatly facilitated these interpretations. Microwave studies of $\mathrm{CO}_{2}-\mathrm{HCl}$ and $\mathrm{CO}_{2}-\mathrm{HF}$ determined linear geometries for these complexes, ${ }^{10-14}$ constraining the reaction to be collinear. In contrast, an infrared diode-laser study of the $\mathrm{CO}_{2}$ asymmetric stretch in $\mathrm{HBr}-\mathrm{CO}_{2}$ concluded that the geometry of the complex is quasi-T-shaped,

[^0]neglecting the position of the H atom. ${ }^{12}$ Such results have been confirmed by a later microwave study that also revealed spectra consistent with a T -shaped $\mathrm{Br}-\mathrm{CO}_{2}$ heavy atom geometry, which consequently affected the reaction dynamics. ${ }^{13}$ The quasi-T-shaped geometry observed in $\mathrm{HBr}-\mathrm{CO}_{2}$ is most likely the consequence of the large dispersion interaction between the very polarizable halogen atom and the $\mathrm{CO}_{2}$, giving a close-packed heavy-atom arrangement. Analogous investigations of the structure of $\mathrm{HI}-\mathrm{CO}_{2}$ have not been available so far, and this has prevented the analysis of regiospecific effects and reaction dynamics for this complex. ${ }^{4,8,9,15,16}$

In this work, we report the microwave spectra of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$, $\mathrm{HI}-{ }^{-12} \mathrm{C}^{18} \mathrm{O}_{2}, \mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$, and $\mathrm{HI}-{ }^{-12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ obtained using pulsed-nozzle Fourier -transform microwave spectroscopy. An optimized model of the intermolecular interaction potential has been generated by morphing the potential energy surface (PES) obtained from ab initio calculations to the measured microwave data. This model has been used to investigate the structure of the complex and to provide new insights into its reactions dynamics.

## 2. Experimental Section

2.1. Experimental Methods. Spectra were obtained at National Institute of Standards and Technology (NIST) using a Balle-Flygare pulsed-molecular-beam, ${ }^{17}$ Fabry-Perot cavity, mini Fourier transform microwave spectrometer, operated in the frequency range between 11 GHz and 20 GHz . Since this instrument has been described previously. ${ }^{18,19}$ Only a brief description relevant to the current experiment will be given here. Microwave radiation is coupled to the center of the mirror via a 0.358 cm semirigid coaxial cable. Two commercial pulsed nozzle molecular beam sources have been used on the

TABLE 1: Observed Transition Frequencies in MHz for $\mathrm{HI}-\mathrm{CO}_{2}$ and Isotopomers ${ }^{a}$

| $J^{\prime}$ | $F^{\prime} J^{\prime \prime}$ | $F^{\prime \prime}$ | $\mathrm{HI-12} \mathrm{C}^{16} \mathrm{O}_{2}$ | $\mathrm{HI}-1{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ | $\mathrm{HI}^{-12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$ | $\mathrm{II}^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ | ${ }^{\prime}$ | $F^{\prime}$ | $J^{\prime \prime} F^{\prime \prime}$ | $\mathrm{HI}-1{ }^{2} \mathrm{C}^{16} \mathrm{O}_{2}$ | HI-12 ${ }^{18} \mathrm{O}_{2}$ | HI- ${ }^{12} \mathrm{C}^{18} \mathrm{O}^{160}$ | $\mathrm{HI}-1 \mathrm{C}^{16} \mathrm{C}^{18} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1_{10}$ | $3 / 21_{01}$ | 5/2 | 11433.722 | 10232.385 |  |  | 312 | $9 / 2$ | 303912 | 11979.218 | 10774.166 |  |  |
| 110 | $7 / 2101$ | 5/2 | 11499.963 | 10298.771 |  |  | 312 |  | $3035 / 2$ | 12034.677 | 10830.155 |  |  |
| $1{ }_{10}$ | $3 / 21_{01}$ | $3 / 2$ | 11625.686 |  |  |  | 312 | 9/2 | $30311 / 2$ | 12092.057 |  |  |  |
| $1{ }_{10}$ | $7 / 21_{01}$ | $7 / 2$ | 11634.995 | 10434.128 |  |  | 313 | $7 / 2$ | $2027 / 2$ | 17393.530 | 15806.783 | 15258.351 | 15269.054 |
| $1{ }_{10}$ | $5 / 21_{01}$ | 7/2 | 11780.711 | 10579.732 |  |  | $3_{13}$ | 9/2 | $2027 / 2$ | 17395.635 | 15809.025 | 15260.459 | 15271.294 |
| 110 | $5 / 21_{01}$ | $3 / 2$ | 11837.639 | 10636.743 |  |  | 313 | $7 / 2$ | $2025 / 2$ | 17422.377 | 15835.441 | 15286.727 | 15298.178 |
| 110 | $5 / 21_{01}$ | 5/2 |  | 10444.377 |  |  | 313 | 5/2 | 202712 | 17445.767 |  | 15310.727 |  |
| 111 | $5 / 200$ | 5/2 | 13410.093 | 12081.343 | 11401.488 | 11421.068 | 313 | 5/2 | $2025 / 2$ | 17474.614 |  | 15339.105 | 15350.313 |
| 111 |  | 5/2 | 13686.201 | 12357.147 | 11674.192 | 11697.509 | 313 |  | 202912 | 17517.371 | 15930.822 | 15380.622 | 15394.739 |
| 111 | $3 / 20_{00}$ | 5/2 | 13806.017 | 12476.518 |  |  | 313 | $3 / 2$ | $2025 / 2$ | 17535.932 |  |  |  |
| 211 | $1 / 2202$ | 3/2 | 11521.917 | 10319.455 |  |  | 313 | 5/2 | 202312 | 17567.101 | 15980.514 | 15430.682 | 15444.124 |
| 211 | 9/2 202 | $7 / 2$ | 11567.722 | 10364.990 |  |  | 313 | 11/2 | 202912 | 17607.822 | 16020.610 | 15471.144 | 15484.373 |
| 211 | $3 / 2202$ | 5/2 | 11595.957 | 10393.019 |  |  | 313 | 3/2 | $2023 / 2$ | 17628.418 | 16041.659 |  | 15505.109 |
| 211 |  | 1/2 | 11603.156 |  |  |  | 313 |  |  | 17709.656 | 16122.955 | 15492.095 |  |
| 211 | 9/2 202 | 9/2 | 11689.458 | 10486.787 |  |  | 313 | $1 / 2$ | $2{ }^{02} 11 / 2$ | 17753.085 | 16165.986 | 15615.624 |  |
| 211 | 5/2 202 | $7 / 2$ | 11756.721 | 10553.985 |  |  | 413 | 3/2 | $4_{04} 3 / 2$ | 11928.333 |  |  |  |
| 211 | $3 / 2202$ | $1 / 2$ | 11769.682 | 10567.047 |  |  | 413 | 5/2 | 404 | 12027.172 |  |  |  |
| 211 | 5/2 202 | 5/2 | 11785.569 | 10582.644 |  |  | 413 | 7/2 | 404712 | 12128.345 |  |  |  |
| 211 |  | $7 / 2$ | 11826.419 | 10623.911 |  |  |  | 11/2 | 404 9/2 | 12162.561 |  |  |  |
| 211 | $7 / 2202$ | 5/2 | 11855.266 | 10652.571 |  |  | 413 | 11/2 | $4_{04} 11 / 2$ | 12177.094 | 10968.801 |  |  |
| 211 |  | 3/2 | 11878.056 | 10675.378 |  |  |  | 7/2 | 404512 | 12194.394 |  |  |  |
| 211 | $7 / 2202$ | 9/2 | 11948.149 | 10745.708 |  |  | 413 |  | 4049 | 12194.876 |  |  |  |
| 212 | $7 / 2101$ | 5/2 | 15416.326 | 13957.962 | 13345.060 | 13359.670 | 413 | 9/2 | $40411 / 2$ | 12209.410 |  |  |  |
| 212 | $5 / 2101$ | 5/2 | 15447.661 | 13989.027 | 13376.343 | 13390.696 |  |  | $4047 / 2$ | 12236.761 |  |  |  |
| 212 | $7 / 2101$ | $7 / 2$ | 15551.360 | 14093.317 | 13478.565 | 13496.655 | 413 | 11/2 | 4041312 | 12282.508 |  |  |  |
| 212 | $5 / 2101$ | $7 / 2$ | 15582.693 |  | 13509.846 |  |  | 13/2 | 404 13/2 | 12008.648 | 10800.201 |  |  |
| 212 | $5 / 2101$ | $3 / 2$ | 15639.623 | 14181.398 | 13566.157 | 13585.385 | 413 | 5/2 | 404312 | 12091.897 |  |  |  |
| 212 | 9/2 $1_{01}$ | 7/2 | 15674.141 | 14215.209 | 13600.986 | 13618.796 | 413 | 5/2 | $4_{04} 7 / 2$ | 11961.122 | 10752.911 |  |  |
| 212 | $3 / 21_{01}$ | $3 / 2$ | 15745.772 | 14287.904 | 13672.182 | 13691.778 | 414 |  | $3037 / 2$ |  | 17573.161 | 17085.317 | 17093.212 |
| 212 | $3 / 21_{01}$ | 5/2 | 15553.808 |  | 13482.367 |  | 414 | 9/2 | 303912 |  |  | 17089.588 | 17096.561 |
| 212 | $1 / 2101$ | $3 / 2$ | 15820.136 |  |  |  |  | 11/2 | 303912 |  | 17584.826 | 17100.765 | 17107.701 |
| 312 | $1 / 2303$ | $3 / 2$ | 11665.385 | 14361.185 | 13746.211 |  | 414 | $7 / 2$ | $3037 / 2$ |  |  | 17119.456 | 17127.014 |
| 312 | $11 / 23_{03}$ | 9/2 | 11705.633 |  |  |  | 414 | $7 / 2$ | $3039 / 2$ |  | 17607.822 |  |  |
| 312 | $1 / 2303$ | 1/2 | 11721.148 |  |  |  |  | $7 / 2$ | $3035 / 2$ |  | 17664.999 | 17178.010 | 17186.507 |
| 312 | $3 / 2303$ | 5/2 | 11724.040 | 10519.564 |  |  | 414 | 13/2 | $30311 / 2$ |  | 17775.117 | 17290.284 | 17299.341 |
| 312 | $3 / 2303$ | $3 / 2$ | 11796.352 | 10591.100 |  |  |  | 5/2 | 303 3/2 |  | 17788.045 | 17301.787 |  |
| 312 | 11/2 303 | 11/2 | 11818.468 | 10613.088 |  |  | 514 | 5/2 | 505 5/2 | 12188.861 |  |  |  |
| 312 | $5 / 2303$ | 5/2 |  | 10690.928 |  |  |  | 11/2 | 404 9/2 |  | 19274.447 | 18854.734 | 18858.014 |
| 312 | 5/2 303 | $7 / 2$ | 11837.726 | 10633.067 |  |  |  | 13/2 | 404 11/2 |  | 19304.402 | 18885.043 | 18887.973 |
| 312 | $3 / 2303$ | 1/2 | 11852.120 |  |  |  |  | 9/2 | 404712 |  | 19341.580 |  |  |
| 312 | $5 / 2303$ | $3 / 2$ | 11967.784 | 10762.463 |  |  |  | 15/2 | $4_{04} 13 / 2$ |  | 19481.335 | 19060.994 | 19066.143 |
| 312 | $7 / 2303$ | $7 / 2$ | 11976.927 |  |  |  | 515 | 5/2 | 404 3/2 |  | 19568.111 |  |  |
| 312 | $7 / 2303$ | 9/2 | 11977.884 |  |  |  |  | 1/2 | 1/2 | 12734.228 |  |  |  |
| 312 | 9/2 303 | $7 / 2$ | 11978.261 |  |  |  |  |  |  |  |  |  |  |

${ }^{a}$ Experimental uncertainties on the transitions are estimated to be $\pm 5 \mathrm{kHz}( \pm 1 \sigma)$.

TABLE 2: Spectroscopic Constants ${ }^{a}$ for $\mathbf{H I}-\mathbf{C O}_{2}$ and Isotopologues/Isotopomers (in $\mathbf{M H z}$ )

|  | $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ |
| :--- | :---: | :---: | :---: | :---: |
| $A$ | $12630.3794(13)^{b}$ | $11365.09291(83)$ | $10654.1037(25)$ | $10678.3653(27)$ |
| $B$ | $1087.4242(16)$ | $1020.78971(86)$ | $1053.9091(26)$ | $1050.7627(26)$ |
| $C$ | $988.07631(54)$ | $923.46000(36)$ | $955.59604(75)$ | $953.15160(77)$ |
| $\Delta_{J K}$ | $0.168020(263)$ | $0.142611(96)$ |  |  |
| $e Q q_{a a, 0}$ | $639.6916(49)$ | $640.7206(58)$ | $632.8231(70)$ | $649.0339(85)$ |
| $e Q q_{a a, 1}$ | $641.621(10)$ | $643.039(10)$ |  |  |
| $\left(e Q q_{b b}-e Q q_{c c}\right)_{0}$ | $-552.52(14)$ | $-544.279(22)$ | $-495.8825(28)$ | $-499.9435(37)$ |
| $\left(e Q q_{b b}-e Q q_{c c}\right)_{1}$ | $-498.9821(19)$ | $-498.5682(21)$ |  |  |
| $\left\|e Q q_{a b}\right\|$ | $250.65(14)$ | $242.49(10)$ | $275.488(98)$ | $210.52(12)$ |
| $\sigma$ | 0.069 | 0.075 | 0.024 | 0.019 |

${ }^{a}$ Fitted using JPL Program, H. M. Pickett, J. Mol. Spectrosc. 1991, 148, 371. ${ }^{b}$ The numbers shown in parenthesis are Type A uncertainties with $K=1$ coverage, i.e., $1 \sigma$.
spectrometer, with sizes of the orifices from 0.3 to 1 mm and beam pulse lengths extending from $100 \mu$ s to 1 ms .

In the present experiments, the gas mixtures are controlled by mass-flow controllers. Typically, one gas mixture consists of HI in Ar and the other of $\mathrm{CO}_{2}$ in Ar , with the mole fractions of HI and $\mathrm{CO}_{2}$ varying from $0.5 \%$ to several units percent. The data from several hundred nozzle pulses are averaged. Typical linewidths are $15-20 \mathrm{kHz}$ and all frequency measurements are estimated to have an uncertainty less than 5 kHz .
2.2. Results. The measured transitions for the $\mathrm{HI}-\mathrm{CO}_{2}$ isotopomers are listed in Table 1 . Only $b$-type, $\Delta K_{\mathrm{a}}=1$ transitions were observed. The individual rotational transitions split into a number of hyperfine components over a broad range of frequency due to the nuclear quadrupole interactions of the $I=5 / 2{ }^{127}$ I nucleus. Figure 1 shows the hyperfine components of the transition $2_{12} \leftarrow 1_{01}$ of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$. In this case, the nine hyperfine components cover a range of 400 MHz . The spectral features were analyzed by fitting the data to a spectrum


Figure 1. Hyperfine components of the transition $2_{12} \leftarrow 1_{01}$ of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$.
generated by the Hamiltonian of a rigid asymmetric rotor: ${ }^{11}$

$$
\begin{align*}
& H_{\mathrm{R}}=\frac{1}{2}\left\{(B+C) J^{2}+\right. \\
& \left.\quad[2 A-(B-C)] J_{a}^{2}+(B-C)\left(J_{b}{ }^{2}-J_{c}^{2}\right)\right\} \tag{2}
\end{align*}
$$

The rotational ladders were supplemented by one centrifugal distortion term using the Watson asymmetric-rotor centrifugaldistortion Hamiltonian written in the $A$-reduced $I^{r}$ representation. ${ }^{20}$

In addition to the rotational Hamiltonian, we also included the ${ }^{127} \mathrm{I}$ nuclear electric quadrupole Hamiltonian $H_{\mathrm{Q}}$. The quadrupole coupling constant is designated by $e Q q,{ }^{21}$ and the general expression for the quadrupole coupling energy is

$$
\begin{align*}
E_{\mathrm{Q}}=\frac{2}{(J+1)(2 J+3)} & \sum_{g=a, b, c} e Q q_{g g}\left(J, i\left|J_{g}^{2}\right| J, i\right) \times \\
& {\left[\frac{\frac{3}{4} C(C+1)-J(J+1) I(I+1)}{2 J(2 J-1) I(2 I-1)}\right] } \tag{3}
\end{align*}
$$

where,
$C=F(F+1)-J(J+1)-I(I+1)$
$F=J+I, J+I-1, J+I-2, \ldots,|J-I|$
Spectra of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ showed a larger number of transitions than those of the two mono- ${ }^{18} \mathrm{O}$ substituted complexes, $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$. In fact, for these last two isotopomers, the observed lines can be assigned to pure rotational transitions within the ground vibrational state of an asymmetric top, characterized by the selection rules $\Delta J=1$ and $\Delta K_{\mathrm{a}}=1$, with $J$ up to 5 . On the contrary, in order to assign
all the transitions observed in the spectra of the ${ }^{16} \mathrm{O}^{16} \mathrm{O}$ and ${ }^{18} \mathrm{O}^{18} \mathrm{O}$ isotopologue complexes, it was necessary to introduce two states into the Hamiltonian (eq 2). However, due to the limited $K_{\mathrm{a}}$ data available, the values of the rotational and centrifugal distortion constants were constrained to be the same for the two states, although each one of those states was characterized by their own set of quadrupole coupling constants $e Q q_{a a}$ and $e Q q_{b b}-e Q q_{c c}$.

As the quadrupole coupling has a large magnitude, the treatment of this interaction required going beyond the usual firstorder approximation by adding off-diagonal terms in the asym-metric-rotor nuclear-quadrupole Hamiltonian for both states.

The results from the fittings of the observed transitions are listed in Table 2. The standard deviations of the fits were in the range $19-75 \mathrm{kHz}$, larger than the experimental precision of $\sim 5 \mathrm{kHz}$. The quality of the fits was better for the two mono${ }^{18} \mathrm{O}$ substituted complexes than that for $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$.

## 3. Structural Determination

3.1. Distance $R$ (Distance between the Centers of Mass of the Two Monomers). The inertial defects derived from the spectra for the mono- ${ }^{18} \mathrm{O}$ substituted complexes are relatively large and positive ( 1.90 and $1.93 \mathrm{uma} \cdot \AA^{2}$ ). Similar values have been found in a number of planar T-shaped complexes, ${ }^{22-24}$ where zero-point vibrations in the van der Waals force field gave rise to such positive and relatively large inertial defects.

Figure 2 shows the geometrical parameters $R, \theta_{\mathrm{OCI}}, \theta_{\mathrm{CIH}}(=$ $\left.180^{\circ}-\theta_{\mathrm{HI}}\right)$ and $\phi$, used in the determination of the structure. The angles $\theta_{\mathrm{OCI}}$ and $\theta_{\mathrm{CIH}}$ describe the orientation of both monomers with respect to the axis containing their centers of mass. The dihedral angle $\phi$ measures the orientation of HI relative to $\mathrm{CO}_{2}$ in the complex. $R$ is the distance between the centers of mass of the two constituents and describes the


Figure 2. Schematic drawing of $\mathrm{HI}-\mathrm{CO}_{2}$ complex showing the coordinates used.
stretching motion of the complex. Also, $R$ depends only on the moment of inertia about the $c$-axis, and can be calculated from ${ }^{25}$

$$
\begin{equation*}
\mu R^{2}=I_{\mathrm{c}}-I_{\mathrm{HI}}-I_{\mathrm{CO}_{2}} \tag{5}
\end{equation*}
$$

where $\mu=M_{\mathrm{HI}} M_{\mathrm{CO}_{2}} /\left(M_{\mathrm{HI}}+M_{\mathrm{CO}_{2}}\right)$ is the reduced mass of the complex and $I_{\mathrm{HI}}$ and $I_{\mathrm{CO}_{2}}$ are the moments of inertia of the monomers, respectively. The values of $\mu, I_{\mathrm{HI}}, I_{\mathrm{CO}_{2}}$, and $R$ for all the isotopomers are listed in Table 3.

The $R$ values obtained for the ground state geometries of $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}, \mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}, \mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$, and $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ complexes are $3.7717(1) \AA, 3.7699(1) \AA, 3.7686(1) \AA$, and $3.7739(1)$ $\AA$, respectively. The difference between the first two values give a decrease by 0.0018 (2) $\AA$ for $R$, which can be attributed to the larger reduced mass of $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ compared to $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$. The value of $R$ for the mono- ${ }^{-18} \mathrm{O}$ substituted complexes should be the average of the $R$ values of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$, i.e., $3.7708 \AA$. For the first mono- ${ }^{18} \mathrm{O}$ substituted complex with a $R$ value of $3.7686 \AA$, the difference is $-0.0022(2) \AA(=$ $3.7686-3.7708)$ and for the other one, $+0.0031(2) \AA(=$ $3.7739-3.7708$ ). These results indicated that for the first complex, the ${ }^{18} \mathrm{O}$ atom is tilted toward the I atom and for the other mono- ${ }^{18} \mathrm{O}$ substituted, the ${ }^{18} \mathrm{O}$ atom is tilted away from the I atom.
3.2. Angle $\theta_{\mathbf{C I H}}$. The projection of the HI quadrupole tensor onto the principal inertia axis of $\mathrm{HI}-\mathrm{CO}_{2}$ results in the following equation, ${ }^{26}$

$$
\begin{equation*}
e Q q_{a a}^{\mathrm{HI}-\mathrm{CO}_{2}}=e Q q^{\mathrm{HI}}\left\langle P_{2}\left(\cos \theta_{2}\right)\right\rangle \tag{6}
\end{equation*}
$$

where $0^{\circ} \leq \theta_{2} \leq 180^{\circ}$ is the angle between the HI axis and the $a$ principal inertia axis of the complex. The $e Q q_{a a}^{\mathrm{HI}-\mathrm{CO}_{2}}$ is the component of the quadrupole coupling constant of the complex as measured along the $a$-axis, and $e Q q^{\mathrm{HI}}$ is the quadrupole coupling of the isolated HI , that is $-1828.286(9) \mathrm{MHz} .{ }^{27}$ The relatively large mass of the iodine atom permits us to consider the angle $\theta_{2}$ as approximately equal to the angle $\theta_{\mathrm{CIH}}$ (Figure 2). To calculate this angle, we used the following approximation: $\left\langle\cos ^{2} \theta_{2}\right\rangle \approx\left(\cos \theta_{2}\right) .^{2}$ The results for the angle $\theta_{\mathrm{CIH}}$ are listed in Table 3.
3.3. Angle $\theta_{\text {OCI }}$. The angle $\theta_{\text {OCI }}$ can be determined using the following equation:

$$
\begin{align*}
& \sin ^{2} \theta_{\mathrm{OCI}}=\frac{I_{a}\left(I_{c}-I_{a}\right)}{I_{1}\left(I_{c}-I_{1}-I_{2}\right)}-\frac{I_{2}}{I_{1}} \sin ^{2} \theta_{\mathrm{CIH}}- \\
& \frac{I_{2}}{\left(I_{c}-I_{1}-I_{2}\right)} \sin ^{2}\left(\theta_{\mathrm{OCI}}+\theta_{\mathrm{CIH}}\right) \tag{7}
\end{align*}
$$

In eq 7 , the use of the moment of inertia along the $a$-axis gave a value of $\theta_{\mathrm{OCI}}$ only for the two mono- ${ }^{18} \mathrm{O}$ substituted complexes. A detailed discussion of the determination of the angle $\theta_{\mathrm{OCI}}$ for pure isotopic complexes is presented in Section 5. The results for the angle $\theta_{\mathrm{OCI}}$ are listed in Table 3 .

## 4. Theoretical Calculations

In this study, we generated a model of the intermolecular potential energy surface of $\mathrm{HI}-\mathrm{CO}_{2}$ by using the potential
morphing methodology that was previously employed for the investigation of $(\mathrm{HBr})_{2}{ }^{28}$ and $\mathrm{OC}-\mathrm{HCl}^{29}$ complexes. Within this procedure, the ab initio potential energy surface of the $\mathrm{HI}-$ $\mathrm{CO}_{2}$ complex is first obtained. Then, the values of the rotational, centrifugal distortion, and $\left\langle P_{2}\left(\cos \theta_{\mathrm{HI}}\right)\right\rangle$ constants are determined by using the calculated rotational energy levels. These values are compared with the experimentally determined ones and the calculated potential energy surface is iteratively adjusted to reproduce the experimental parameters with the minimum root-mean-square deviation. Each step is described in detail below.
4.1. Ab Initio Calculation of the Intermolecular Potential. The intermolecular potential energy surface was generated by assuming that the geometries of the monomers $\mathrm{CO}_{2}$ and HI were linear and rigid. In all the calculations, the bond length of HI was fixed at the experimental value $r_{e}=1.6092 \AA \AA^{30}$ The $\mathrm{C}-\mathrm{O}$ bond length in $\mathrm{CO}_{2}$ was taken to be $r_{e}=1.1625 \AA$, which is undistinguishable from the $r_{0}$ value within the experimental error. ${ }^{31}$ As a consequence of this approximation, the original nine-dimensional (9-D) vibrational model was reduced to a four-dimensional (4-D) model. The interaction potential of HI$\mathrm{CO}_{2}$ complex was therefore expressed in terms of the Jacobi coordinates ( $R, \theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi$ ), as used in the analysis of the experimental data (Figure 2). ${ }^{32}$

The ab initio interaction energy of the complex was calculated at the coupled cluster singles and doubles with perturbated triples $[\operatorname{CCSD}(\mathrm{T})]$ level of theory, within the nonrelativistic approximation, by using the MOLPRO 2006 electronic structure package. ${ }^{33}$ The augmented correlation consistent polarized valence triple- $\zeta$ basis set (aug-cc-pVTZ) ${ }^{34,35}$ was used for all the atoms except for the iodine, for which the basis set was aug-cc-pVTZ-pp. ${ }^{36}$ Every calculated point was corrected for the basis set superposition error (BSSE) using the counterpoise correction of Boys and Bernardi. ${ }^{37}$ The potential energy surface was calculated on a grid, built taking nine different $R$ points (from $3.500 \AA$ to $8.000 \AA$ ), five points for both $\theta_{\mathrm{OCI}}$ and $\theta_{\mathrm{HI}}$ (from $0^{\circ}$ to $180^{\circ}$ ), and 10 points for $\phi$ (from $0^{\circ}$ to $360^{\circ}$ ). This set of points was supplemented with a selection of 20 specific angular points ( $\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi$ ) for each value of $R$, giving a final grid composed of 2430 points. To have a global representation of the surface, the angular dependence of the calculated PES was fitted to a spherical expansion ${ }^{32}$ for each value of $R_{j}$. A weighting factor $F_{\mathrm{w}}=75.0 \mathrm{~cm}^{-1}$ was used in order to obtain an absolute average difference less than $6.0 \mathrm{~cm}^{-1}$ between the values of the points in the ab initio and fitted potentials for the points within $250.0 \mathrm{~cm}^{-1}$ of the minimum of the potential. ${ }^{32}$ More details of the fitting procedure have been given elsewhere. ${ }^{32,38}$ The 4-D potential was obtained by interpolating the angular potential on the grid of $R_{j}$ points at fixed angular coordinates using a one-dimensional radial reproducing kernel. ${ }^{32,38}$

The 4-D ab initio PES has two equivalent global minima with well depth of $421.7 \mathrm{~cm}^{-1}$ at the geometries $R=4.000 \AA, \theta_{\text {OCI }}$ $=73.8^{\circ}, \theta_{\mathrm{HI}}=120.3^{\circ}, \phi=0.0^{\circ}$, and $R=4.000 \AA, \theta_{\mathrm{OCI}}=$ $106.2^{\circ}, \theta_{\mathrm{HI}}=120.3^{\circ}, \phi=180.0^{\circ}$.
4.2. Calculation of Rotational Energy Levels. The rotational energy levels were calculated using the 4-D PES by the pseudospectral approach, discussed previously. ${ }^{32,38}$ The experimental value of the rotational constants $B_{0}$ for the isolated monomers were used in the expression of the kinetic energy for all the calculations. ${ }^{39,40}$ The accuracy of the resulting eigenvalues was controlled by the following parameters: ${ }^{32} R_{\text {start }}$ $=3.500 \AA$ (the first point of the radial grid), $R_{\text {end }}=8.000 \AA$ (the last point), $N_{\mathrm{R}}=38$ (the number of grid points in the radial direction), $N_{\theta \mathrm{OCI}}=48$ and $N_{\theta \mathrm{HI}}=24$ (the numbers of $\theta_{\mathrm{OCI}}$ and

TABLE 3: Structural Parameters for $\mathbf{H I}-\mathbf{C O}_{2}$ and Its Isotopologues/Isotopomers

|  | $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$ | $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mu$ (uma) | 32.73281 | 34.90168 | 33.82974 | 33.82974 |
| $I_{\mathrm{HI}}\left(\mathrm{uma} \cdot \AA^{2}\right)^{a}$ | 2.62463594(26) |  |  |  |
| $I_{\mathrm{CO}_{2}}\left(\mathrm{uma} \cdot \AA^{2}\right)^{\text {b }}$ | 43.200165(8) | 48.606358(14) | 45.785466(12) | 45.785466(12) |
| $I_{C}\left(\right.$ uma $\left.\cdot \AA^{2}\right)$ | 511.47386(27) | 547.23960(36) | 528.85945(42) | 530.21576(43) |
| $R$ ( ${ }_{\text {A }}$ ) | $3.771714(38)$ | $3.769924(30)$ | $3.768557(58)$ | $3.773873(57)$ |
| $e Q_{\text {a }} \mathrm{H}^{\mathrm{H}-\mathrm{CO}_{2}}(\mathrm{MHz})$ | 639.6916(49) | 640.7206(58) | 632.8231(70) | 649.0339(85) |
| $\theta_{\text {CIH }}(\mathrm{deg})$ | 71.55(1) | 71.59 (1) | 71.32 (1) | 71.89(1) |
| $\theta_{\text {HI }}$ (deg) | 108.45(1) | 108.41(1) | 108.68(1) | 108.11(1) |
| $\theta_{\text {OCI }}(\mathrm{deg})$ | $82.30(1)^{c}$ | $82.51(1)^{c}$ | 82.15(1) | 82.56(1) |

${ }^{a}$ From ref 27. ${ }^{b}$ From ref 35. ${ }^{c}$ Estimated value (discussed in Section 5).

TABLE 4: Experimental Data Used in the Fits and Fitted Values with the Uncertainties Used

| isotopomer | observable | units | $V_{\text {ab initio }}$ | $V_{\text {morphed }}$ | exp | $\sigma_{\mathrm{k}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ | A | $\mathrm{cm}^{-1}$ | 0.459 | 0.416 | 0.421 | 0.003 |
|  | $(B+C) / 2$ | $10^{-2} \mathrm{~cm}^{-1}$ | 3.191 | 3.462 | 3.462 | 0.002 |
|  | $\Delta_{J K}$ | $10^{-8} \mathrm{~cm}^{-1}$ | 2325.8 | 520.0 | 560.5 | 10.0 |
|  | $\left\langle P_{2}\left(\cos \theta_{\mathrm{HI}}\right)\right\rangle(\mathrm{HI})$ |  | -0.317 | -0.351 | -0.350 | 0.001 |
| $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ | $A$ | $\mathrm{cm}^{-1}$ | 0.414 | 0.374 | 0.379 | 0.003 |
|  | $(B+C) / 2$ | $10^{-2} \mathrm{~cm}^{-1}$ | 2.989 | 3.243 | 3.243 | 0.002 |
|  | $\Delta_{J K}$ | $10^{-8} \mathrm{~cm}^{-1}$ | 2483.8 | 520.4 | 475.7 | 10.0 |
|  | $\left\langle P_{2}\left(\cos \theta_{\mathrm{HI}}\right\rangle\right\rangle(\mathrm{HI})$ |  | -0.316 | -0.351 | -0.350 | 0.001 |
| $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}^{16} \mathrm{O}$ | $A$ | $\mathrm{cm}^{-1}$ | 0.362 | 0.358 | 0.355 | 0.003 |
|  | $(B+C) / 2$ | $10^{-2} \mathrm{~cm}^{-1}$ | 3.093 | 3.354 | 3.351 | 0.002 |
|  | $\left\langle P_{2}\left(\cos \theta_{\mathrm{HI}}\right)\right\rangle(\mathrm{HI})$ |  | -0.309 | -0.345 | -0.346 | 0.001 |
| $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}$ | $A$ | $\mathrm{cm}^{-1}$ | 0.363 | 0.360 | 0.356 | 0.003 |
|  | $(B+C) / 2$ | $10^{-2} \mathrm{~cm}^{-1}$ | 3.084 | 3.340 | 3.342 | 0.002 |
|  | $\left\langle P_{2}\left(\cos \theta_{\mathrm{HI}}\right)\right\rangle(\mathrm{HI})$ |  | -0.324 | -0.357 | -0.355 | 0.001 |
|  | $G$ |  | 101.50 | 1.96 |  |  |

TABLE 5: Optimized Values for the Parameters of the Morphing Functions

| $\alpha$ | $i$ | $\lambda_{\alpha, i}=\left(\begin{array}{llllll}l_{x} & n & \theta_{\mathrm{OCI}} & \theta_{\mathrm{HI}} & \phi\end{array}\right)$ | $C_{\alpha, i}^{0}$ | $C_{\alpha, i}$ | $\sigma$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| 1 | 1 | 0 |  |  |  |  | 1.0 | 1.0433 | 0.0084 |
| 2 | 1 | 0 |  |  |  |  | 1.0 | $(1.0)$ | constrained |
| 3 | 1 | 0 |  |  |  | 0.0 | 0.03804 | 0.00017 |  |
| 1 | 2 | 2 | 2 | 90 | 90 | 0 | 0.0 | 0.2181 | 0.0039 |

$\theta_{\mathrm{HI}}$ points used in the grid), and $N_{\phi}=54$ (the number of $\phi$ points). The number of radial functions and radial spectral basis functions is $N_{\mathrm{F}}=34$. All of the summations over spectral states are truncated so that $j_{\mathrm{CO}_{2}} \leq j_{\max }=26$ and $j_{\mathrm{HI}} \leq j_{\max }=22$ include all possible values of $m_{\mathrm{CO}_{2}}$ and $m_{\mathrm{HI}}$. The tolerance used to determine the convergence of the eigenvalues in the Lanczos procedure was $10^{-12}$.
4.3. Morphing the Ab Initio Potential. The ab initio potential, $V_{\mathrm{ab}}$ initio $\left(R, \theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)$, was morphed using the transformation

$$
\begin{align*}
& V_{\text {morphed }}\left(R, \theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)=S_{1}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right) \times \\
& V_{\text {ab initio }}\left(S_{2}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)\left(R-R_{\mathrm{F}}\right)+\right. \\
& \left.\quad\left[1+S_{3}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)\right] R_{\mathrm{F}}, \theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right) \tag{8}
\end{align*}
$$

where,

$$
\begin{equation*}
S_{\alpha}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)=\sum_{i} C_{\alpha, i} F_{\lambda \alpha, i}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right) \tag{9}
\end{equation*}
$$

In eq $9, C_{\alpha, i}$ are the morphing parameters and $F_{\lambda}$ are the angular morphing functions ${ }^{28,29}$ labeled by the index $\lambda=\left(l_{x}, n\right.$, $\theta^{\prime}{ }_{\text {OCI }}, \theta_{\mathrm{HI}}^{\prime}, \phi^{\prime}$ ). In this work, we used $n=2$ and angular

TABLE 6: Predicted Spectroscopic Constants Form the Morphed Potential for $\mathrm{DI}^{-12} \mathrm{C}^{16} \mathrm{O}_{2}$

| observable | units | value |
| :--- | :--- | :--- |
| $A$ | $\mathrm{~cm}^{-1}$ | 0.361 |
| $(B+C) / 2$ | $10^{-2} \mathrm{~cm}^{-1}$ | 3.460 |
| $\left\langle P_{2}\left(\cos \theta_{\mathrm{DI}}\right)\right\rangle(\mathrm{DI})$ |  |  |

morphing functions with $l_{x}=0$ and 2. The morphing functions are then given by

$$
\begin{align*}
F_{\lambda}\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right)= & {\left[N_{\lambda} \sum_{l_{\mathrm{OCI}}=0}^{l_{x}} \sum_{l_{\mathrm{HI}}=0}^{l_{x}} \sum_{m=-\min \left(l_{\mathrm{OCI}} l_{\mathrm{HII}}\right)}^{\min \left(l_{\mathrm{oCI}}, l_{\mathrm{HH}}\right)} I_{l_{\mathrm{OCl},} l_{\mathrm{H},}, m}\right.} \\
& \left.\left(\theta_{\mathrm{OCI}}, \theta_{\mathrm{HI}}, \phi\right) I_{l_{\mathrm{OCl}} l_{\mathrm{HI}}, m}\left(\theta_{\mathrm{OCI}}^{\prime}, \theta_{\mathrm{HI}}^{\prime}, \phi^{\prime}\right)\right]^{n} \tag{10}
\end{align*}
$$

The value of $N_{\lambda}$ is chosen so that $F_{\lambda}\left(\theta^{\prime}{ }_{\mathrm{OCI}}, \theta_{\mathrm{HI}}^{\prime}, \phi^{\prime}\right)=1$. The $F_{\lambda}$ are defined so that they approach Dirac delta functions located at $\left(\theta_{\text {OCI }}^{\prime}, \theta_{\mathrm{HI}}^{\prime}, \phi^{\prime}\right)$ as $l_{x}$ increases with $n=1$. In the present study, the value of $R_{\mathrm{F}}$ was selected to be $3.900 \AA$. The morphing parameters were obtained by a regularized nonlinear least-squares optimization ${ }^{41}$ using the regularization parameter $\gamma=10.0$. The quality of the fit of the experimental data was evaluated by computing the value of the root-mean-square (rms) deviation from the experimental data

$$
\begin{equation*}
G(\gamma)=\left[\frac{1}{M} \sum_{k=1}^{M}\left\{\frac{O_{k}^{\mathrm{expt}}-O_{k}^{\mathrm{calc}}\left(C_{\alpha, i}(\gamma)\right)}{\sigma_{k}}\right\}^{2}\right]^{1 / 2} \tag{11}
\end{equation*}
$$

4.4. Results. The experimental data used to morph the PES of $\mathrm{HI}-\mathrm{CO}_{2}$ complex are reported in Table 4. The PES was morphed using three morphing functions, two with no angular dependence $\left(l_{x}=0\right)$ and one localized angular function with $l_{x}$


Figure 3. Morphed potential of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ (left side of the figure) with the corresponding statistical uncertainties (right side of the figure), relative to the minimum of the potential which occurs at $R=3.780 \AA, \theta_{\mathrm{OCI}}=77.9^{\circ}, \theta_{\mathrm{HI}}=114.3^{\circ}$, and $\phi=0.0^{\circ}$, with $V=-457(14) \mathrm{cm}^{-1}$. All contours are given in $\mathrm{cm}^{-1}$.
$=2$ (Table 5). During the fitting procedure, the morphing parameter $C_{2,1}$ was not included as it could not be determined
with statistical significance and did not change the quality of the final fit. The final rms after the morphing was $G=1.96$


Figure 4. Probability densities of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ in the ground state (left side of the figure) with energy of $E=340.954 \mathrm{~cm}^{-1}$ and in the first excited state (right side of the figure) with energy of $E=340.917 \mathrm{~cm}^{-1}$. All contours are given in arbitrary units.
and indicates an improved agreement with the experimental data when compared to the original ab initio data with $G=101.50$.

In Figure 3, two-dimensional slices of the morphed potential of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ are shown in the left column and the
corresponding estimated errors relative to global minimum are shown in the right column. Two equivalent global minima with a well depth of $457(14) \mathrm{cm}^{-1}$ were determined, corresponding to the geometries $R=3.780 \AA, \theta_{\mathrm{OCI}}=77.9^{\circ}, \theta_{\mathrm{HI}}=114.3^{\circ}$,


Figure 5. Probability densities of $\mathrm{DI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ in the ground state (left side of the figure) with energy of $E=361.687 \mathrm{~cm}^{-1}$ and in the first excited state (right side of the figure) with energy of $E=361.686 \mathrm{~cm}^{-1}$. All contours are given in arbitrary units.
$\phi=0.0^{\circ}$, and $R=3.780 \AA, \theta_{\mathrm{OCI}}=102.1^{\circ}, \theta_{\mathrm{HI}}=114.3^{\circ}$, $\phi=180.0^{\circ}$, separated by a barrier of $181(17) \mathrm{cm}^{-1}$. The top of the barrier was located at the geometry $R=3.818 \AA, \theta_{\text {OCI }}=$
$90.0^{\circ}, \theta_{\mathrm{HI}}=98.1^{\circ}, \phi=90.0^{\circ}$, which corresponds to a T-shaped geometry with the hydrogen located out-of-plane. Also the morphed potential has a secondary minimum with a well
depth of $405(14) \mathrm{cm}^{-1}$, at the geometry $R=3.875 \AA, \theta_{\text {OCI }}=$ $124.4^{\circ}, \theta_{\mathrm{HI}}=35.4^{\circ}, \phi=0.0^{\circ}$. The probability densities of $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ for the ground state and first excited-state are given in Figure 4.

## 5. Discussion

In Section 3, the calculation of the angles $\theta_{\mathrm{CIH}}$ and $\theta_{\mathrm{OCI}}$ from our experimental results was discussed. This calculation led to a quasi-T-shaped geometry with two sets of supplementary angles. The morphed potential has been used to select the correct set of angles, shown on Figure 4, which correspond to the experimental values $\theta_{\mathrm{OCI}}=82.30(1)^{\circ}$ and $\theta_{\mathrm{CIH}}=71.55(1)^{\circ}$. In the previous analysis on $\mathrm{HBr}-\mathrm{CO}_{2}^{12}$, the angle $\theta_{\mathrm{CBrH}}$ was determined by considering the experimental value of the $\mathrm{D} / \mathrm{H}$ rotational constants, which implied that the proton was directed away from the $\mathrm{CO}_{2}$ monomer. On the contrary, the present analysis indicates that the proton is directed toward the $\mathrm{CO}_{2}$ unit in the $\mathrm{HI}-\mathrm{CO}_{2}$ complex. We could not observe lines for the $\mathrm{DI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ complex. However, we were able to predict the values of the spectroscopic constants of $\mathrm{DI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ based on the morphed potential (Table 6). The probability densities of $\mathrm{DI}-{ }^{-12} \mathrm{C}^{16} \mathrm{O}_{2}$ for the ground state and first excited state are given in Figure 5.

In Table 2, we have compared the values of the rotational constant $A$ of $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ with the values of the mono- ${ }^{18} \mathrm{O}$ substituted complexes. It may be noticed that the values of $A$ in $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ are significantly larger that those in the mono- ${ }^{18} \mathrm{O}$ substituted complexes. This difference is not commensurate with an isotopic effect but can be interpreted as a consequence of the hindered rotation of the HI monomer in the $\mathrm{HI}-\mathrm{CO}_{2}$ complex. The hindered rotation of the HI monomer can occur via two significant pathways: in-plane and out-of-plane. On the basis of the morphed potential, the most probable pathway for the hindered rotation occurs out-of-plane, around the $a$-axis of the molecule as described by the angle $\phi$ (Figure 4). Along this pathway, the estimated height of the barrier is $181(17) \mathrm{cm}^{-1}$, which compares with the value of $184 \mathrm{~cm}^{-1}$ for $\mathrm{HBr}-\mathrm{CO}_{2} .^{12}$ This gives the following values for the frequency of tunneling through the barrier: $0.037 \mathrm{~cm}^{-1}$ for $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}, 0.035 \mathrm{~cm}^{-1}$ for $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$, and $0.001 \mathrm{~cm}^{-1}$ for $\mathrm{DI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$. As a consequence of the Bose-Einstein statistics of the spin-zero oxygen nuclei, only symmetric states were allowed for the ground vibrational state for even $K_{\mathrm{a}}$ and only antisymmetric states for odd $K_{\mathrm{a}}$. Consequently, rotation-tunneling transitions were observed for the complexes $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$. Thus, the observed discrepancy in the rotational constant $A$ can be attributed to the allowed transitions in the symmetric complexes from the $K_{\mathrm{a}}=0$ symmetric state to the $K_{\mathrm{a}}=1$ antisymmetric state. Therefore, the rotational constant $A$ for the symmetric complexes will have a larger magnitude by the value of the tunneling splitting, which was not directly determined in this experiment.

By using the value of the $A$ rotational constant for the mono${ }^{18} \mathrm{O}$ substituted complexes in eqs 12 and 13 , it is possible to estimate the $A$ rotational constant for both $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$.

$$
\begin{align*}
& A\left(\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}\right)=\frac{A\left(\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}\right) \times I_{16012 \mathrm{Cl} 18 \mathrm{O}}}{I_{16012 \mathrm{C} 160}}  \tag{12}\\
& A\left(\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}\right)=\frac{A\left(\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}^{18} \mathrm{O}\right) \times I_{16012 \mathrm{Cl} 180}}{I_{18012 \mathrm{C} 180}} \tag{13}
\end{align*}
$$

The calculated values for $A$ are $11304.55(1) \mathrm{MHz}(0.377(1)$ $\mathrm{cm}^{-1}$ ) for $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $10047.21(1) \mathrm{MHz}\left(0.335(1) \mathrm{cm}^{-1}\right)$
for $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$. With these values, the corresponding inertial defects are 2.23 and 2.00 uma $\cdot \AA^{2}$, respectively, which are close to the ones previously determined for the mono- ${ }^{-18} \mathrm{O}$ substituted complexes. It is also possible to estimate the tunneling frequencies, which are $1325.83(1) \mathrm{MHz}\left(0.044(1) \mathrm{cm}^{-1}\right)$ for $\mathrm{HI}-$ ${ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $1317.87(1) \mathrm{MHz}\left(0.043(1) \mathrm{cm}^{-1}\right)$ for $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$. These values can be compared with the tunneling frequency of $\mathrm{HBr}-\mathrm{CO}_{2}{ }^{12}$ of $1200 \mathrm{MHz}\left(0.040 \mathrm{~cm}^{-1}\right)$. The value of the $\theta_{\mathrm{OCI}}$ angle can be reevaluated using eq 7 and the estimated $A$ rotational constants with the tunneling frequency accounted for. The determined values are $82.30(1)^{\circ}$ for $\mathrm{HI}-{ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ and $82.51-$ (1) ${ }^{\circ}$ for $\mathrm{HI}-{ }^{12} \mathrm{C}^{18} \mathrm{O}_{2}$ (Table 3), in agreement with those determined for the mono- ${ }^{-18} \mathrm{O}$ substituted complexes. In the case of the mono- ${ }^{18} \mathrm{O}$ substituted complexes, our morphed potential confirms the picture of pure rotational spectra observed in the experimental data. As the oxygen atoms are not equivalent, the tunneling does not occur.

We determined a minimum energy of $457(14) \mathrm{cm}^{-1}$ for $\mathrm{HI}-$ $\mathrm{CO}_{2}$ from the surface obtained with the optimized intermolecular potential. In the $\mathrm{HX}: \mathrm{CO}_{2}$ homologous series, values were obtained for $\mathrm{CO}_{2}-\mathrm{HF}, \mathrm{CO}_{2}-\mathrm{HCl}$, and $\mathrm{HBr}-\mathrm{CO}_{2}$, respectively, $837 \mathrm{~cm}^{-1}, 576 \mathrm{~cm}^{-1}$, and $397 \mathrm{~cm}^{-1}$, using a potential function developed by Muenter. ${ }^{42}$ For $\mathrm{HBr}-\mathrm{CO}_{2}$, a full ab initio calculation at MP2 level provided a value of $392 \mathrm{~cm}^{-1} .{ }^{12}$ The dissociation energy $D_{0}$ was also obtained from our morphed potential, namely $340.954 \mathrm{~cm}^{-1}$. For comparison, the dissociation energy for $\mathrm{CO}_{2}-\mathrm{HF}$ was experimentally determined with a value of $672(4) \mathrm{cm}^{-1},{ }^{43}$ and for $\mathrm{CO}_{2}-\mathrm{HCl}$, Oudejans et al. gave a rough estimate of $430 \mathrm{~cm}^{-1} .{ }^{44}$

## 6. Conclusions

In the present work, the microwave spectrum of $\mathrm{HI}-\mathrm{CO}_{2}$ has been analyzed to obtain spectroscopic parameters and the geometry of this complex. The experimental data were used to morph the ab initio potential energy surface of $\mathrm{HI}-\mathrm{CO}_{2}$ in order to obtain an optimized intermolecular potential. The determined surface is characterized by two equivalent global minima with a well depth of $457(14) \mathrm{cm}^{-1}$, corresponding to the geometries $R=3.780 \AA, \theta_{\mathrm{OCI}}=77.9^{\circ}, \theta_{\mathrm{HI}}=114.3^{\circ}, \phi=0.0^{\circ}$, and $R=$ $3.780 \AA, \theta_{\mathrm{OCI}}=102.1^{\circ}, \theta_{\mathrm{HI}}=114.3^{\circ}, \phi=180.0^{\circ}$, separated by a barrier of $181(17) \mathrm{cm}^{-1}$. Also, the morphed potential has a secondary minimum with a well depth of $405(14) \mathrm{cm}^{-1}$ at the geometry $R=3.875 \AA, \theta_{\mathrm{OCI}}=124.4^{\circ}, \theta_{\mathrm{HI}}=35.4^{\circ}, \phi=$ $0.0^{\circ}$. The determined structure is now available for interpreting regiospecific effects in photoinitiated reaction dynamics of the $\mathrm{HI}-\mathrm{CO}_{2}$ complex and its clusters.

The ground state geometry of the complex is planar, with the heavy atoms having a quasi-T-shape configuration, with geometry $\theta_{\mathrm{OCI}}=82.30(1)^{\circ}$ and $\theta_{\mathrm{CIH}}=71.55(1)^{\circ}$. This quasi-T-shaped geometry differs significantly from the one observed in $\mathrm{HBr}-\mathrm{CO}_{2}{ }^{13}$ and the linear geometries found for $\mathrm{CO}_{2}-\mathrm{HCl}^{10}$ and $\mathrm{CO}_{2}-\mathrm{HF} .{ }^{14} \mathrm{An}$ interesting feature revealed by the morphed PES of $\mathrm{HI}-\mathrm{CO}_{2}$ is that the complex has a linear $\mathrm{OCO}-\mathrm{HI}$ geometry when the separation of the monomers is large (i.e., $R$ $=6.000 \AA$ ). In addition, when the distance between the monomers is shorter than the equilibrium distance (i.e., $R=$ $3.000 \AA$ ), the complex has a T-shaped geometry with $\theta_{\text {OCI }}=$ $92.0^{\circ}, \theta_{\mathrm{HI}}=96.1^{\circ}$, and $\phi=0.0^{\circ}$. The model obtained in the present study is also directly relevant to furthering an understanding of photoinitiated $\mathrm{H}_{n} \mathrm{X}: \mathrm{CO}_{2}$ complexes $(\mathrm{X}=\mathrm{I}, \mathrm{Br}, \mathrm{Cl}$, $n=1$ and $\mathrm{X}=\mathrm{S}, n=2$ ) reactions.

Acknowledgment. We gratefully acknowledge the financial support of the National Science Foundation through grants

DMS-0216275 and CHE-0613202 and as well as from CACE(TAMU). John W. Bevan thanks the Robert A. Welch Foundation (grant no. A747) for financial support. We also thank Lisa M. Pérez for assistance in the ab initio calculations.

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